



LIBS – PRINCIPES PHYSIQUES FONDAMENTAUX

Arnaud BULTEL[‡]

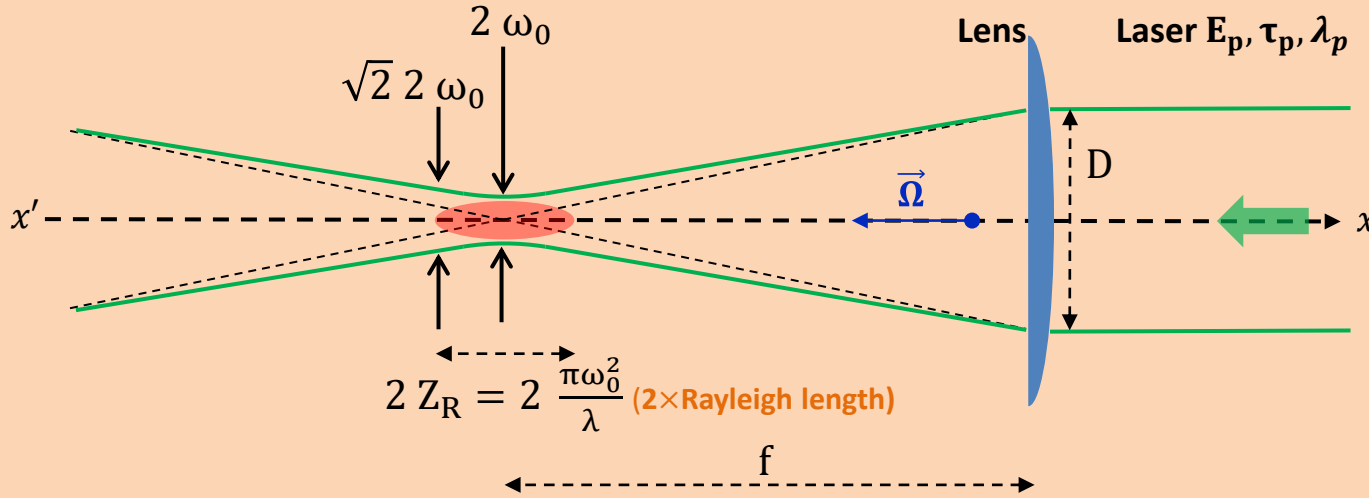
Outline

- 1. Laser-Sample Interaction**
- 2. Dynamics of the Expansion – Shockwave**
- 3. Departure from Equilibrium (McWhirter and Co.)**

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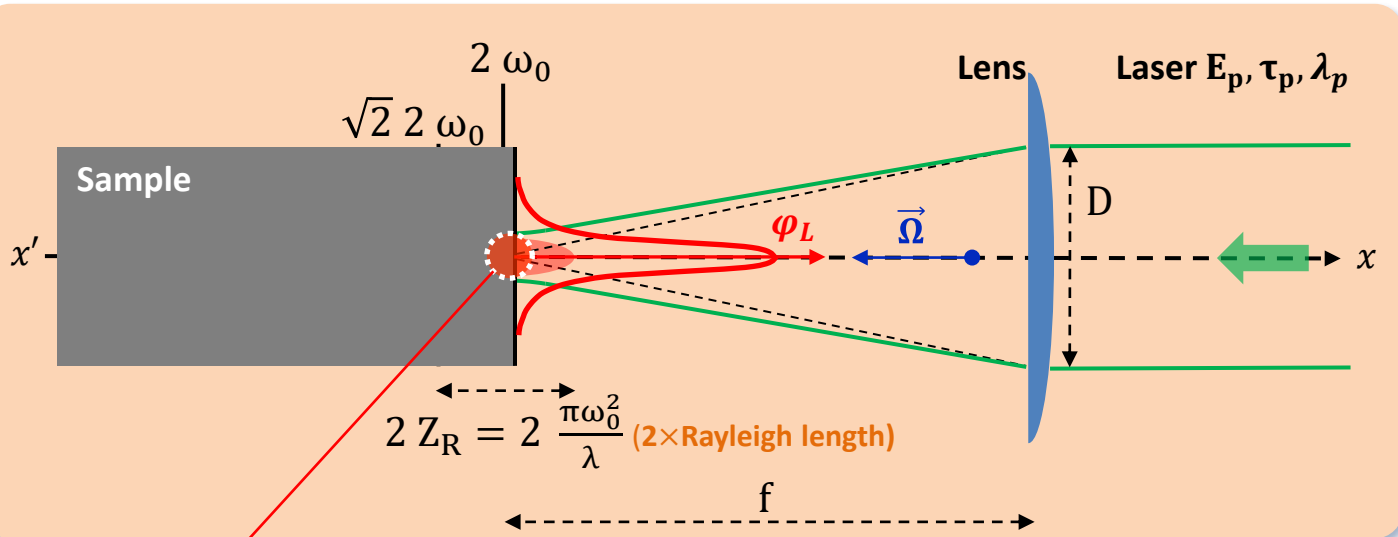
Laser-sample interaction...



Variable	Typical values
E_p (mJ)	10
τ_p (ns)	5
λ_p (nm)	532, 1064
D (mm)	4
f (cm)	10
ω_0 (μm)	100
$\Delta\sigma$ (cm^{-1})	0.01
φ_L (Wm^{-2})	$10^{13} - 10^{14}$
L_L ($\text{Wm}^{-2}\text{sr}^{-1}\text{m}^{-1}$)	$10^{16} - 10^{17}$

$$L_L \sim \underbrace{\frac{E_p}{\tau_p} \frac{1}{\pi \omega_0^2} \frac{4f^2}{\pi D^2}}_{\varphi_L} \Delta\sigma$$

Laser-sample interaction...

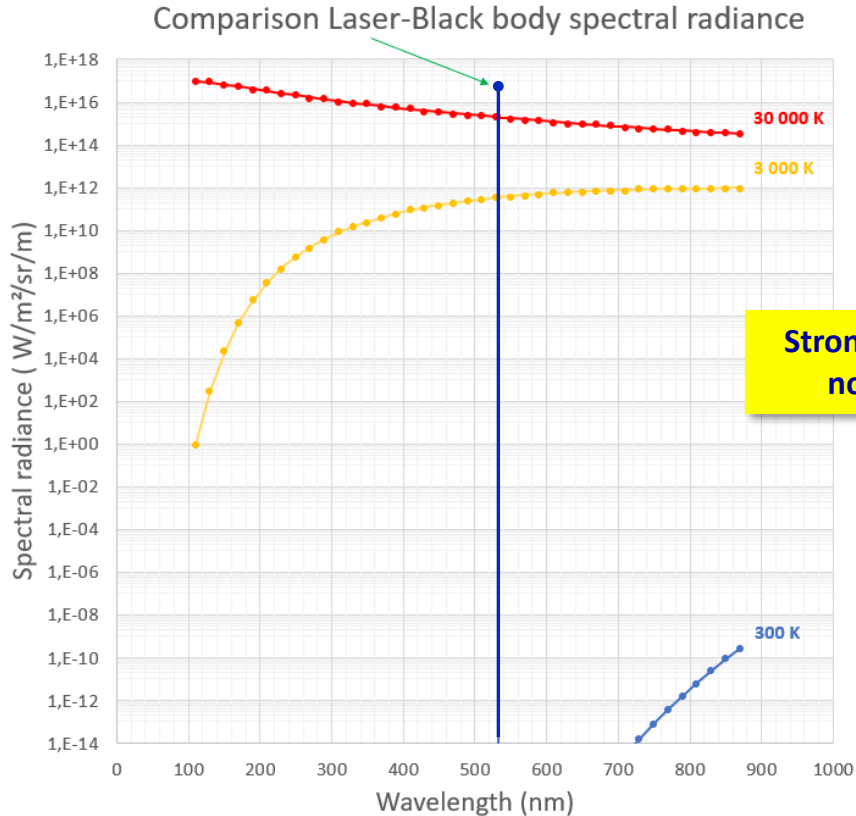


Radiative transfer
within the sample...

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Radiation within the sample...



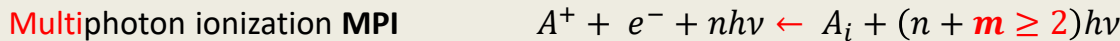
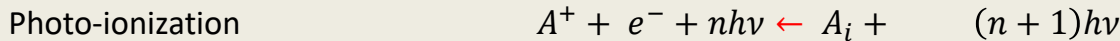
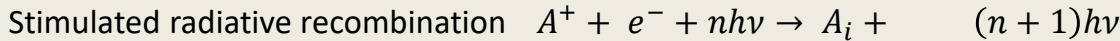
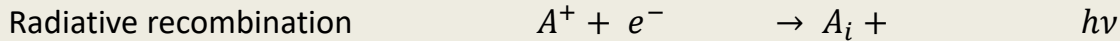
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$$L_L \sim \underbrace{\frac{E_p}{\tau_p} \frac{1}{\pi\omega_0^2}}_{\varphi_L} \frac{4f^2}{\pi D^2} \Delta\sigma$$

Photon-particle interaction within the sample...

Photons are bosons!!!

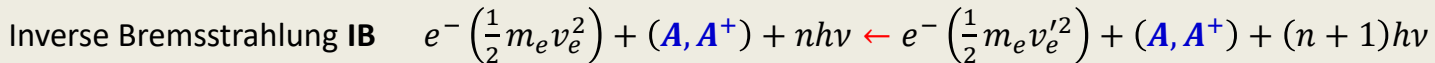
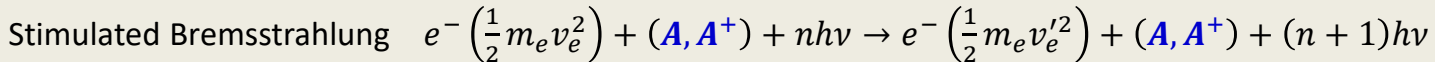
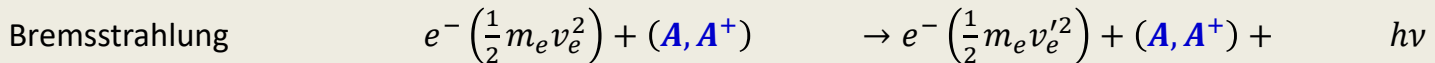
Radiative recombination



All these processes are governed by the Planck's law

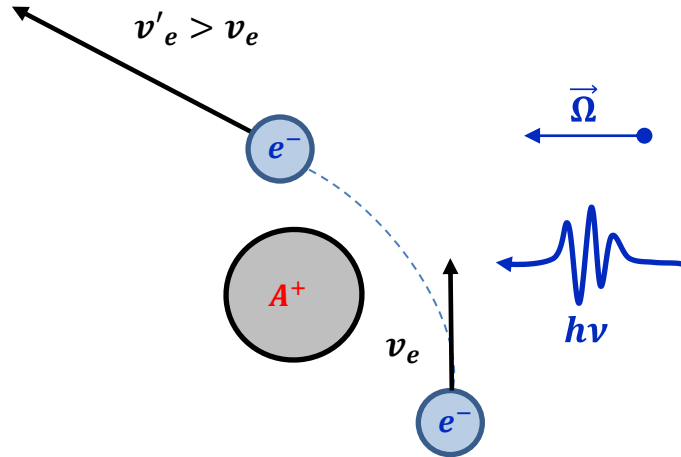
If the sample is dielectric

Bremsstrahlung



⇒ Increase in the volumic electron energy e_e ...

Inverse Bremsstrahlung...



Since T_e is locally defined ($\tau_p \gg \tau_{ee} \approx 10^{-14} s$)...

$$\left(\frac{\partial e_e}{\partial t}\right)_{IB} = \frac{3}{2} n_e k_B \left(\frac{\partial T_e}{\partial t}\right)_{IB} = K_{A^+}(x, t) n_e [A^+] \varphi_L(x, t) \quad (W m^{-3})$$

$$K_{A^+}(x, t) = \frac{4}{3} \left(\frac{e^2}{4\pi \epsilon_0}\right)^3 \sqrt{\frac{2\pi}{3 m_e k_B T_e(x, t)}} \frac{G}{m_e h c^4} \lambda_p^3 \quad (m^5)$$

Since T_{A^+} is locally defined ($\tau_p \gg \tau_{A^+A^+} \approx 10^{-14} s$)...

$$\left(\frac{\partial e_{A^+}}{\partial t}\right)_{EC} = \frac{3}{2} [A^+] k_B \left(\frac{\partial T_{A^+}}{\partial t}\right)_{EC} = \frac{3}{2} [A^+] k_B \frac{T_e - T_{A^+}}{\tau_{A^+-e}} \quad (W m^{-3})$$

$$\tau_{A^+-e} = \left[n_e \frac{\sqrt{2\pi}}{m_e m_{A^+}} \left(\frac{e^2}{4\pi \epsilon_0}\right)^2 \frac{\ln(\Lambda_{A^+-e})}{\left(\frac{k_B T_e}{m_e} + \frac{k_B T_{A^+}}{m_{A^+}}\right)^{3/2}} \right]^{-1} \approx 10^{-12} s$$

$\tau_{A^+-e} \ll \tau_p$ if ns, $\tau_{A^+-e} \gg \tau_p$ if fs

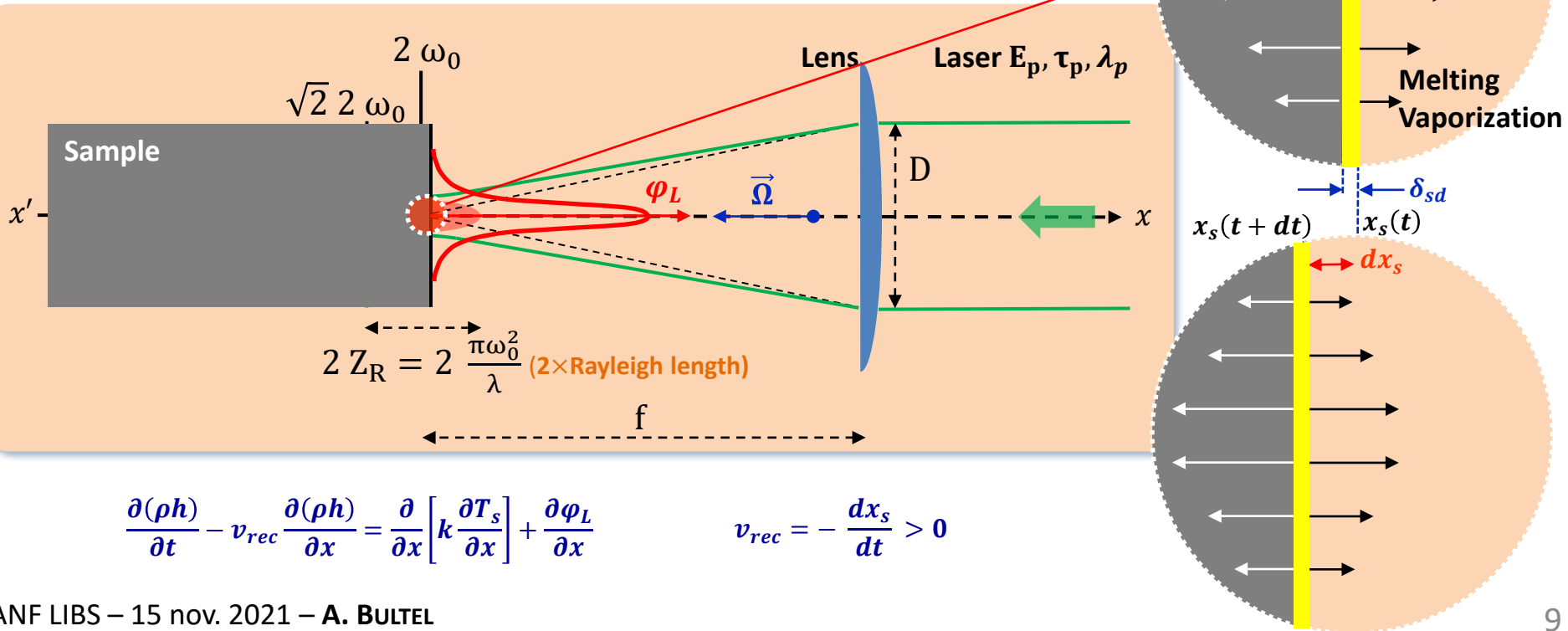
Photons disappear...

$$\frac{1}{c} \frac{\partial L_L}{\partial t} + \vec{\Omega} \overrightarrow{\text{grad}} L_L = \frac{L_L}{c} \quad (W m^{-4} sr^{-1}) \text{ with } L_L < 0 \text{ (also scattering ...)}$$

$$\overrightarrow{\text{grad}} L_L = -\vec{\Omega} \frac{L_L(0, t)}{\delta_{sd}}$$

$$\delta_{sd} = \frac{\lambda_p}{2\pi k_{RI}} \approx 10^{-8} m \quad (\text{skin depth})$$

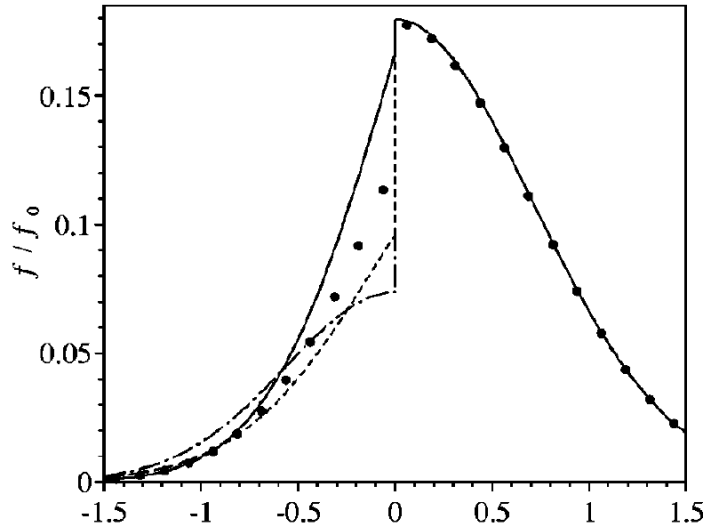
Laser-sample interaction...



Very fast vaporization...

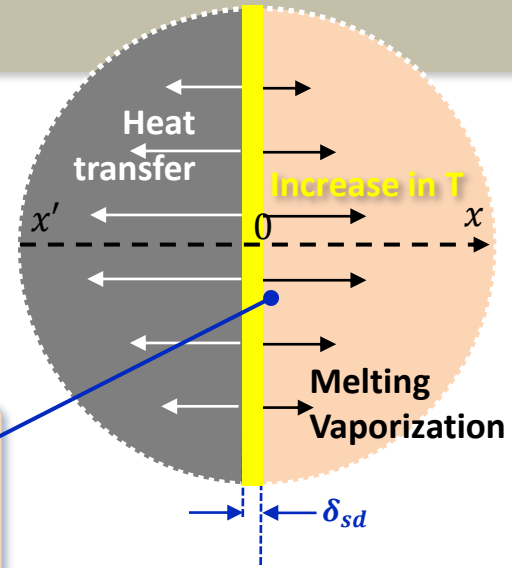
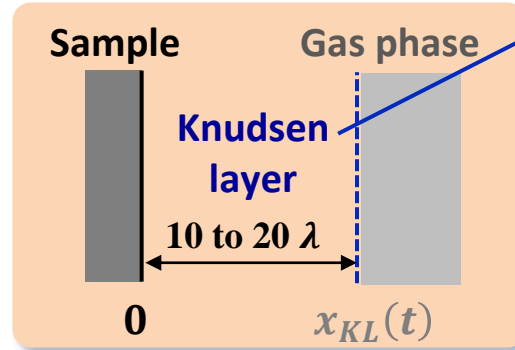
$$T_s < 0.9 T_c$$

T_s much higher than the temperature in the gas phase...



A.V. Gusarov et al
[Phys. Fluids 14 \(2002\) 4242](#)

$$v_x / \sqrt{\frac{2 k_B T_s(0, t)}{m}}$$



Non-equilibrium on the surface...

$$T_s < 0.9 T_c$$

Relationship between S and KL conditions \rightarrow Mach \mathcal{M}_{KL}

\mathcal{M}_{KL}	ρ_{KL}/ρ_s	T_{KL}/T_s	p_{KL}/p_s
0	1	1	1
0.05	0.927	0.980	0.908
0.1	0.861	0.960	0.827
0.2	0.748	0.922	0.690
0.4	0.576	0.851	0.490
0.6	0.457	0.785	0.358
0.8	0.371	0.725	0.269
1.0	0.308	0.669	0.206

Clausius-Clapeyron equation

$$p_s(T_s) = p_{atm} \exp\left[\frac{\Delta h_b m}{k_B} \left(\frac{1}{T_b} - \frac{1}{T_s}\right)\right]$$

$$0.9 T_c < T_s < T_c$$

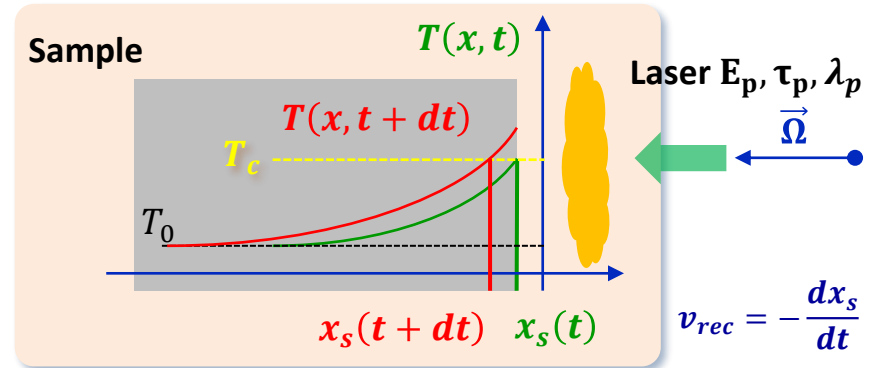
Formation of μ -bubbles within the liquid

\rightarrow Explosive boiling lasting more than the laser pulse

$$T_s > T_c ?$$

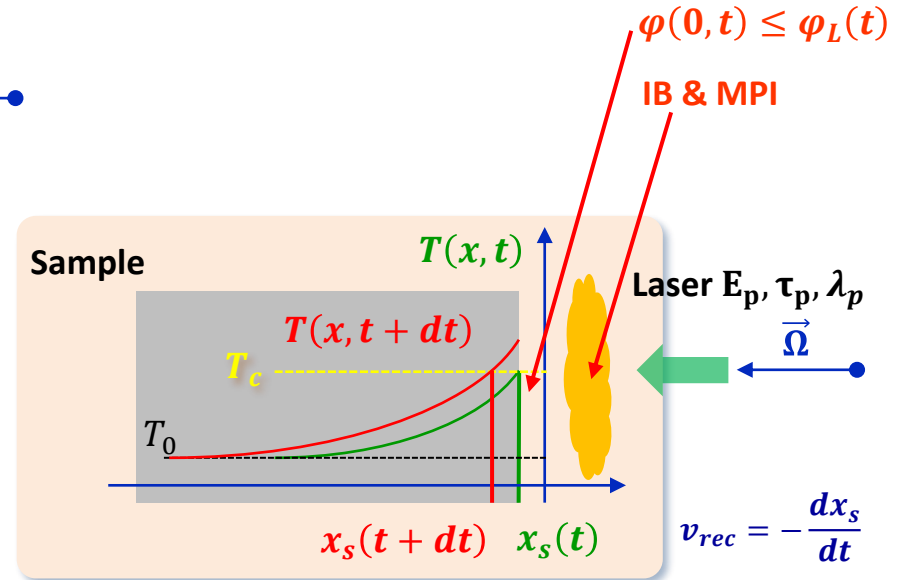
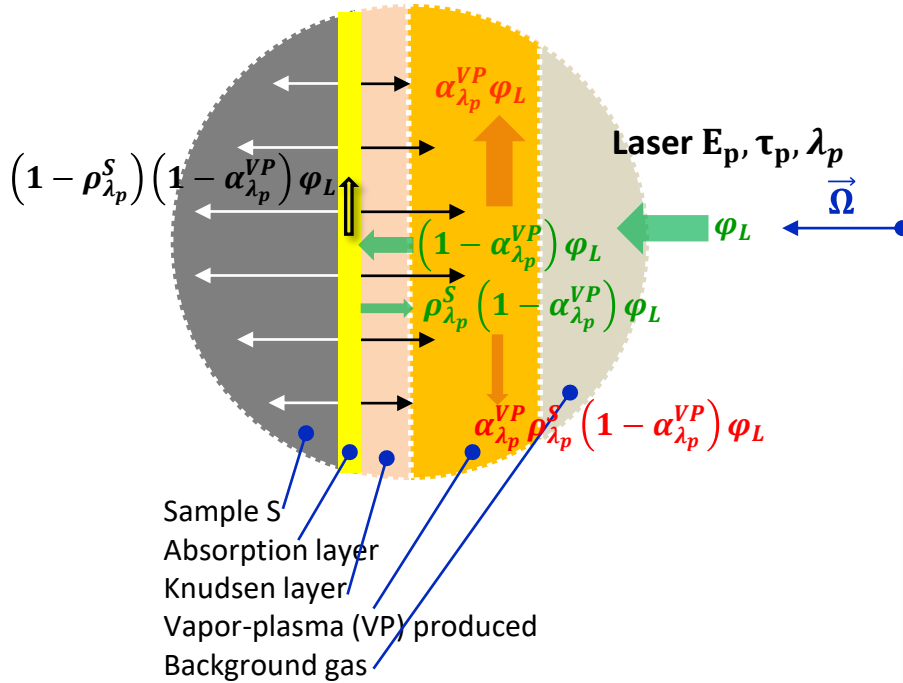
Not phase change anymore \rightarrow Supercritical fluid

This supercritical fluid can be overheated...



Phase non-equilibrium

Screening of the laser pulse by the vapor-plasma produced...



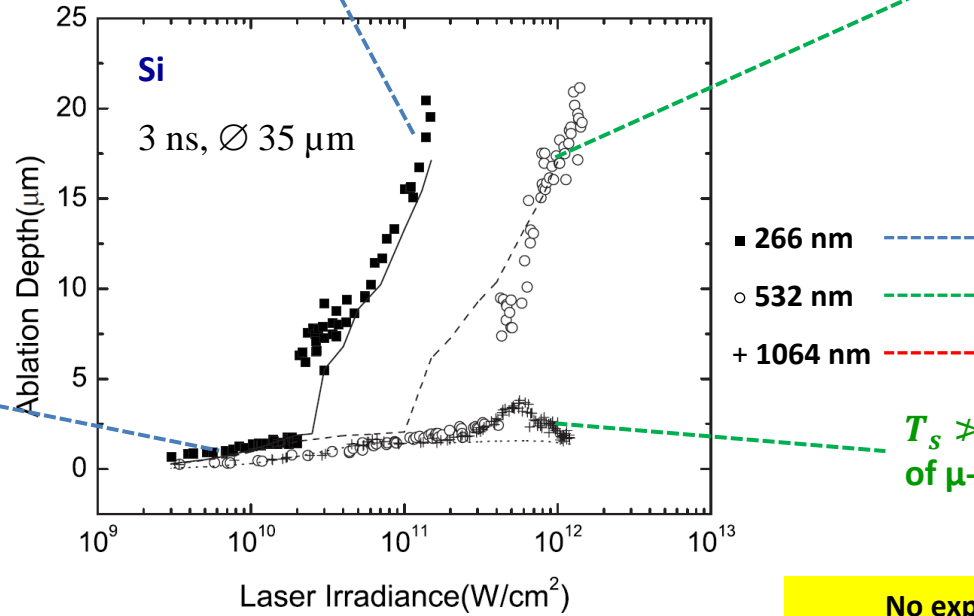
Ablation process...

$T_s > 0.9 T_c$ during the time of μ -bubbles growth

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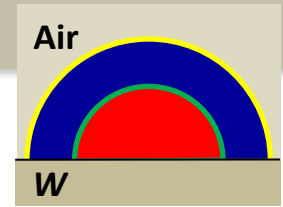
Q. Lu et al. *J. Appl. Phys.* **104** (2008) 083301

No explosive boiling for 1064 nm because of IB efficiency

Outline

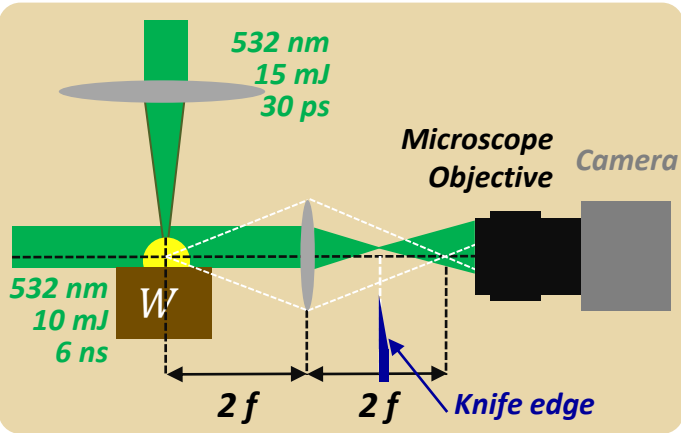
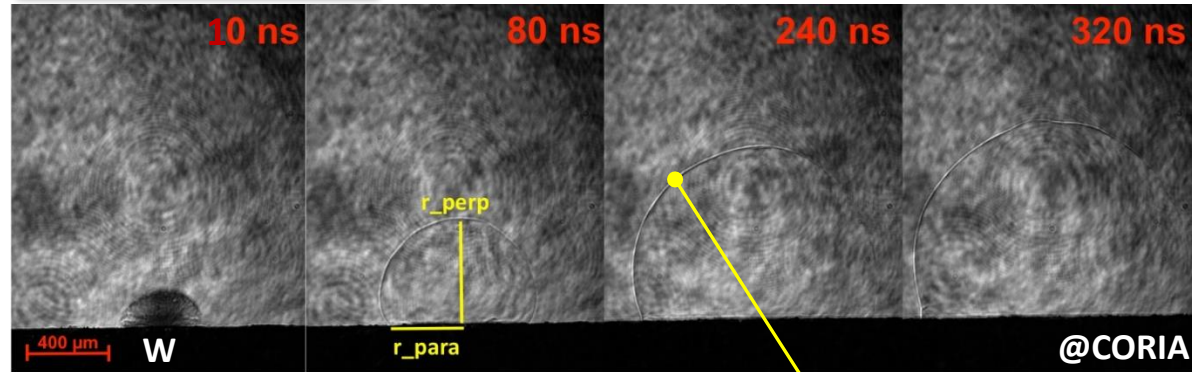
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Interaction with a background gas...



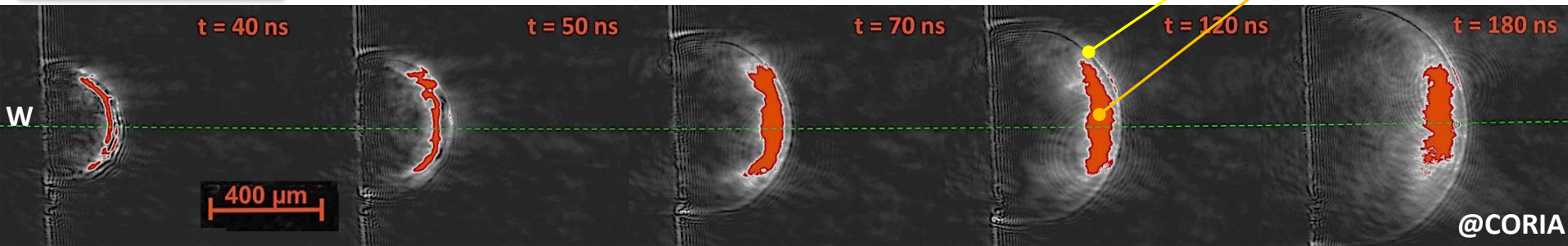
Laser shadowgraphy

Sensitive to $\frac{\partial^2 n}{\partial z^2}$

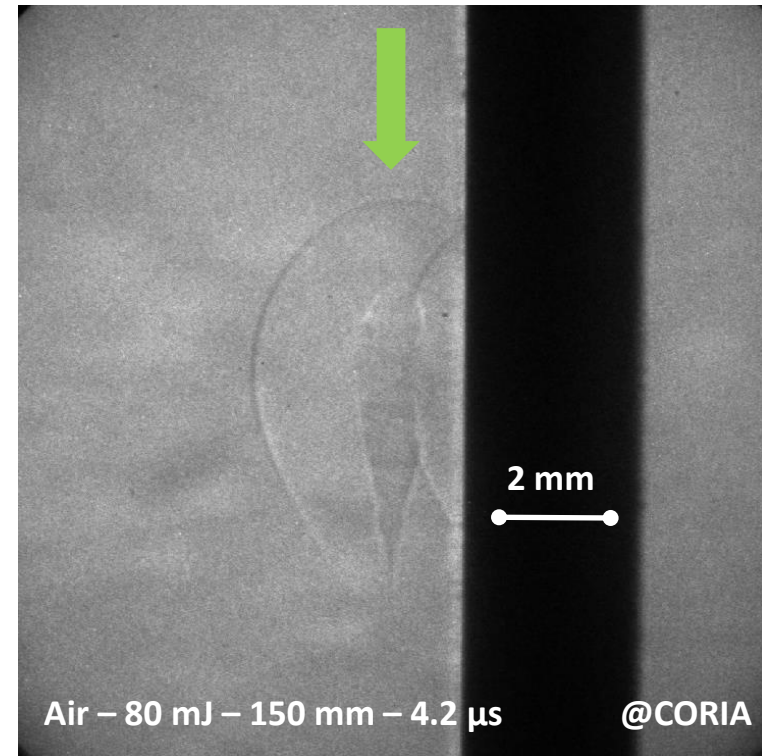
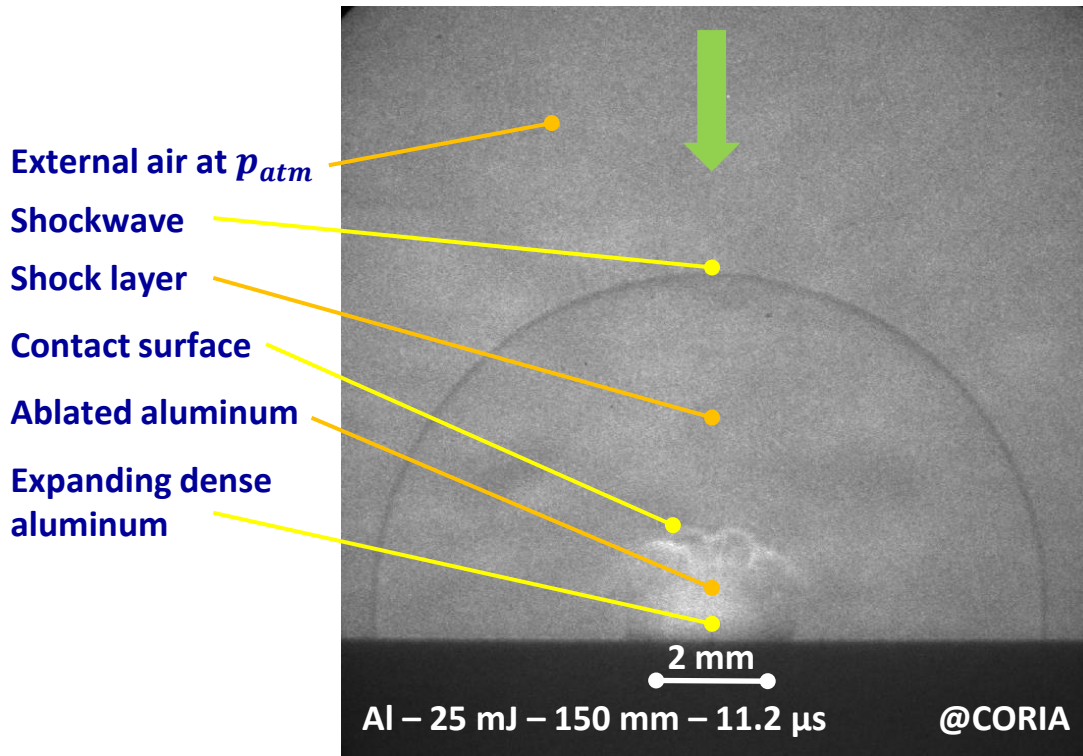


Schlieren Imagery

Sensitive to $\frac{\partial n}{\partial z}$

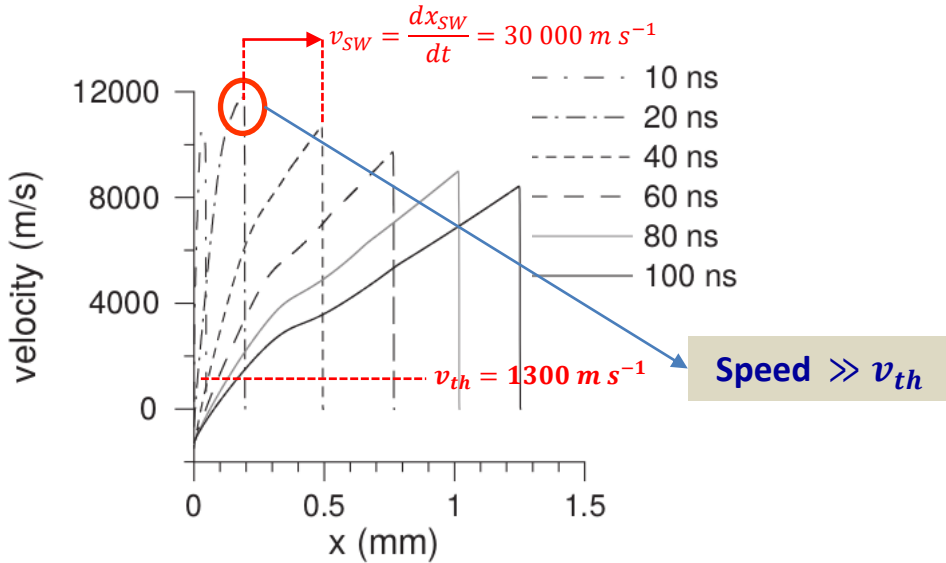


Interaction with a background gas...



Induced expansion...

Distribution of the plasma local speed with time

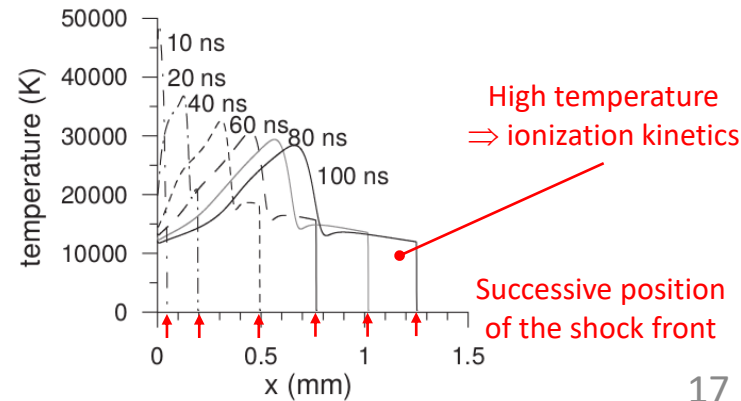
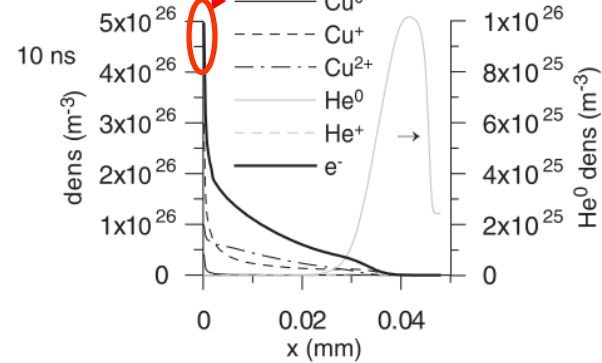


Cu in He (p_{atm}), $\varphi_L = 10^{13}\text{ W m}^{-2}$, $\lambda_L = 266\text{ nm}$, $\tau_L = 5\text{ ns}$

A. Bogaerts et al. [Spectrochim. Acta Part B 60 \(2005\) 1280](#)

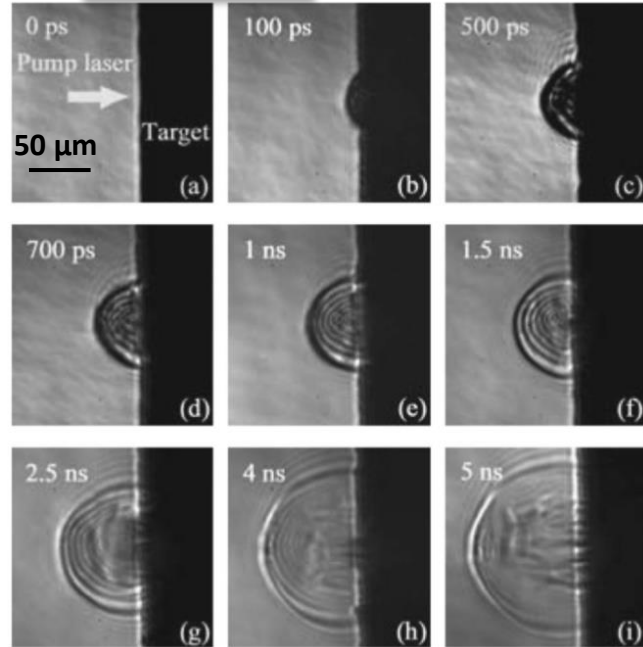
Shorter times:
screening by inverse
Bremsstrahlung

Distribution of densities and temperature with time



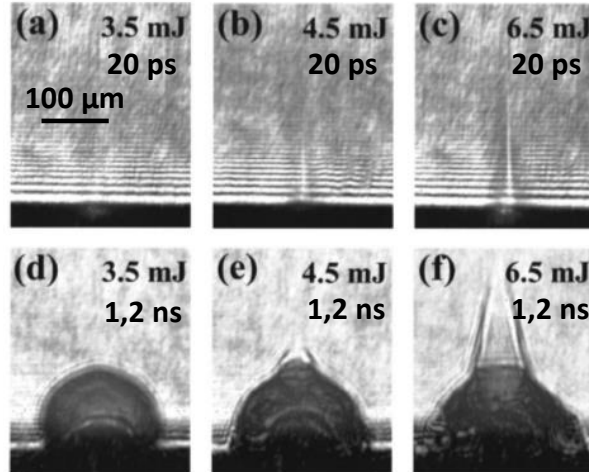
Successive position
of the shock front

Structure...



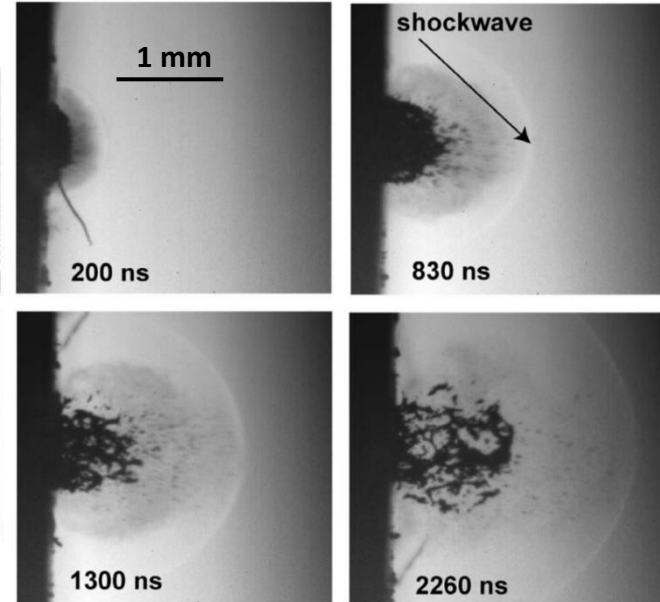
50 fs
800 nm
40 J cm⁻²
Al

N. Zhang *et al.*
[Phys. Rev. Lett. 99 \(2007\) 167602](#)



35 ps
1064 nm
~ 50 J cm⁻²
Cu

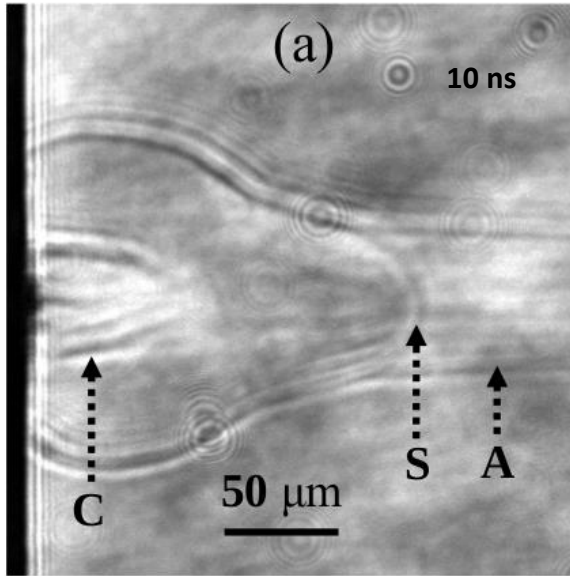
S.S. Mao *et al.*
[Appl. Phys. Lett. 77 \(2000\) 2464](#)



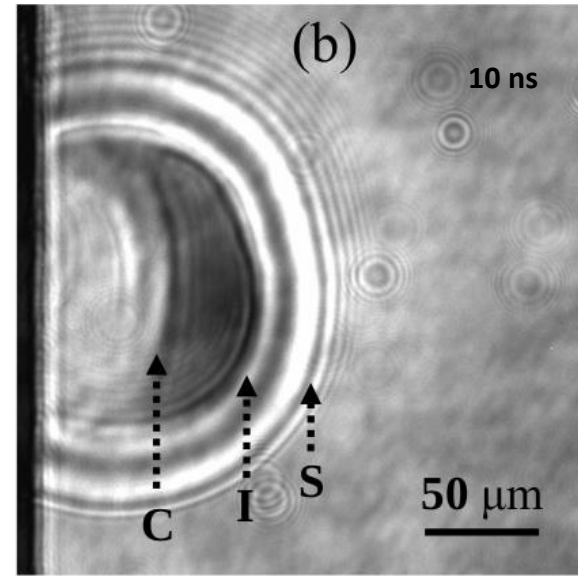
6 ns
1064 nm
6,5 J cm⁻²
Polymère

M. Hauer *et al.*
[Opt. Las. Eng. 43 \(2005\) 545](#)

Structure...



100 fs
266 nm
11 J cm⁻²
Si (air)



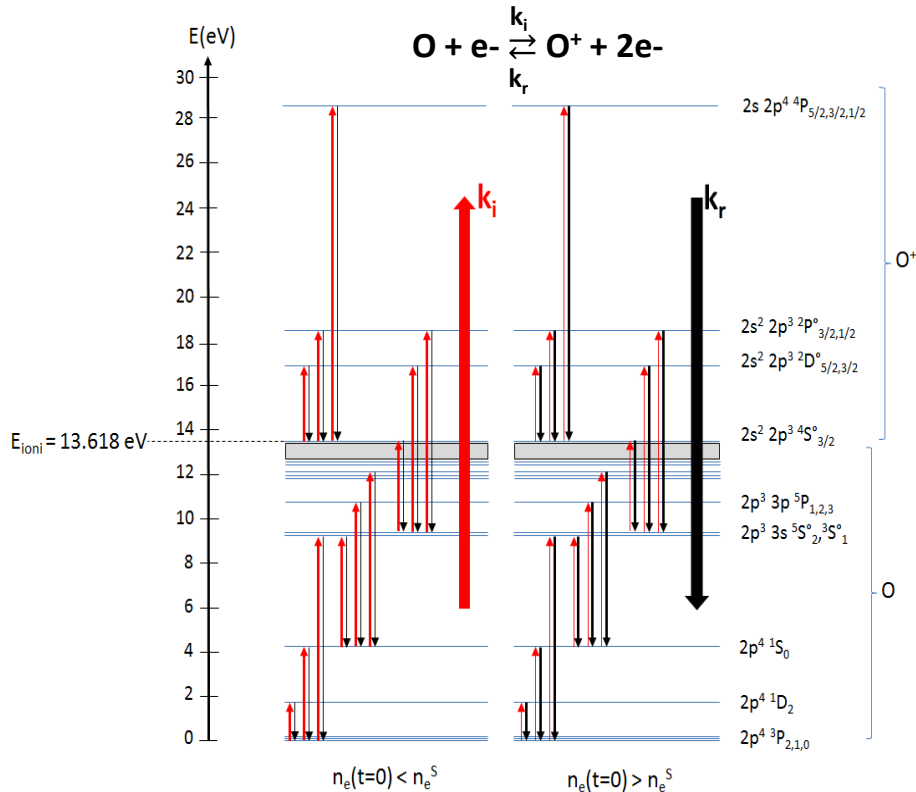
3 ns
266 nm
11 J cm⁻²
Si (air)

X. Zeng *et al.*
Lawrence Berkeley National Lab. (2004)

Outline

1. Laser-Sample Interaction
2. Dynamics of the Expansion – Shockwave
3. **Departure from Equilibrium (McWhirter and Co.)**

Kinetics of ionization – Example



Individual X_m variation rate

$$\begin{aligned} \frac{1}{V} \frac{dN_{X_m}}{dt} = & - \sum_{n>m} k_{m \rightarrow n} \left(1 - \frac{[X_n]}{[X_m]K_{n,m}^B} \right) [X_m] n_e \\ & + \sum_{n<m} k_{n \rightarrow m} \left(1 - \frac{[X_m]}{[X_n]K_{m,n}^B} \right) [X_n] n_e \\ & - \sum_i k_{m \rightarrow i}^+ \left(1 - \frac{[X_i^+] n_e}{[X_m] K_{i,m}^S} \right) [X_m] n_e \end{aligned}$$

Individual X_i^+ variation rate

$$\begin{aligned} \frac{1}{V} \frac{dN_{X_i^+}}{dt} = & - \sum_{j>i} k_{i \rightarrow j} \left(1 - \frac{[X_j^+]}{[X_i^+] K_{j,i}^B} \right) [X_i^+] n_e \\ & + \sum_{j<i} k_{j \rightarrow i} \left(1 - \frac{[X_i^+]}{[X_j^+] K_{i,j}^B} \right) [X_j^+] n_e \\ & + \sum_m k_{m \rightarrow i}^+ \left(1 - \frac{[X_i^+] n_e}{[X_m] K_{i,m}^S} \right) [X_m] n_e \end{aligned}$$

Global X variation rate

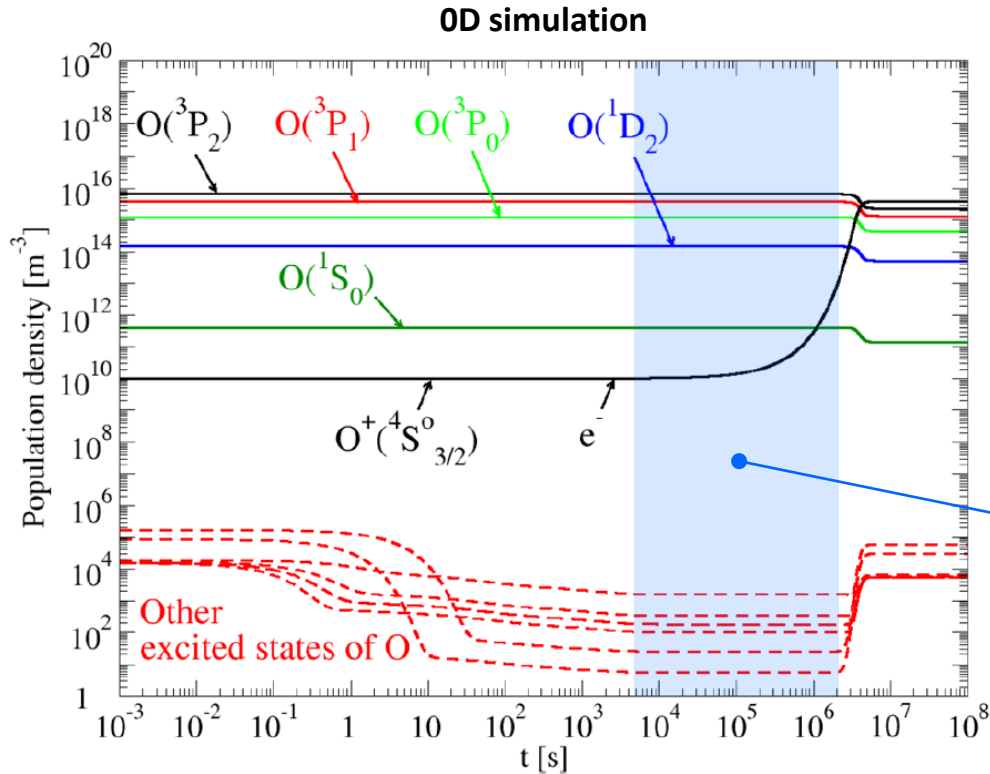
$$\frac{1}{V} \frac{dN_X}{dt} = \sum_m \frac{1}{V} \frac{dN_{X_m}}{dt} = \begin{cases} -k_i [X] n_e \\ +k_r [X^+] n_e^2 \end{cases}$$

Global X^+ variation rate

$$\frac{1}{V} \frac{dN_{X^+}}{dt} = \sum_i \frac{1}{V} \frac{dN_{X_i^+}}{dt} = \begin{cases} +k_i [X] n_e \\ -k_r [X^+] n_e^2 \end{cases}$$

J. Annaloro, V. Morel, A. Bultel *et al.*
[Phys. Plasmas **19** \(2012\) 073515](https://doi.org/10.1088/1742-5122/19/07/073515)

Kinetics of ionization – Example



$T_e = 6000$ K

$n_e(t=0) = 10^{10} \text{ m}^{-3}$ $p = 10^{-3} \text{ Pa}$

$T_{\text{exc}}(t=0) = 6000$ K

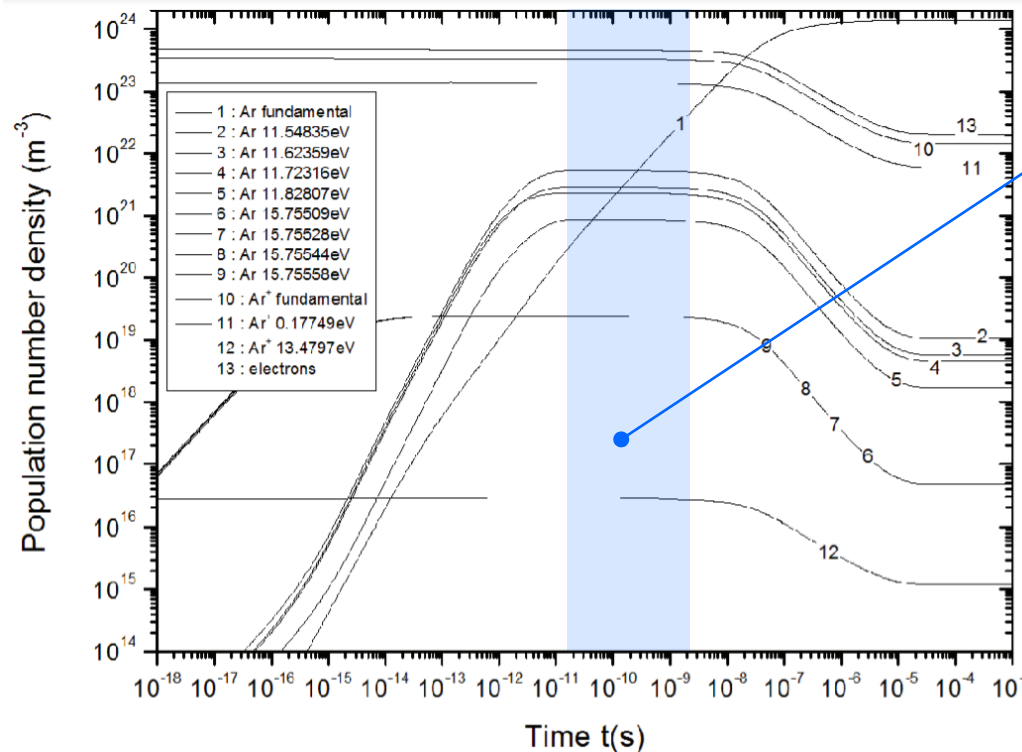
Quasi Steady State QSS

J. Annaloro, V. Morel, A. Bultel *et al.*

[Phys. Plasmas **19** \(2012\) 073515](https://doi.org/10.1088/1742-6596/19/1/013001)

Kinetics of recombination – Example

Behaviour of the excited states



Quasi Steady State QSS

$p_{atm}, 10\ 000\ K$

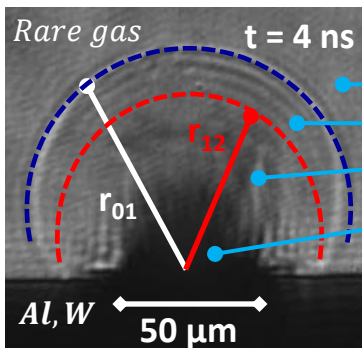
J. Annaloro, P. Teulet, A. Bultel *et al.*
[Eur. Phys. J. D **71** \(2017\) 342](#)

The ECHREM* code

* Eulerian Chemically Reactive
Multi-component plasma code



Assumptions



Hypersonic hemispherical expansion

- (0) External gas (rare gas: Ne, Ar, Kr or Xe)
- (1) Shock layer (shocked rare gas)
- (2) Central plasma (ablated W ou Al)

Ablated material

- r_{01} shock front radius
- r_{12} contact surface radius
- v_{sf} shock front speed

Bi-layer model

Propagation of the shockwave
Rankine-Hugoniot assumption

Atoms and ions... at T_A
Electrons... at T_e

Balance equations

(1) Shock layer

Mass $\rho_0 v_{sf} = \rho_1 [v_{sf} - u_1(r_{01})] \Leftrightarrow \frac{d\rho(\{Rg\}_j^{Z+})}{dt} = \dot{\rho}(\{Rg\}_j^{Z+}) - \frac{\rho(Rg_j^{Z+})}{\rho_1} \frac{d\rho_1}{dt}$

Energy $\epsilon_0 + \frac{p_0}{\rho_0} + \frac{v_{sf}^2}{2} = \epsilon_1 + \frac{p_1}{\rho_1} + \frac{[v_{sf} - u_1(r_{01})]^2}{2}$

Momentum $p_0 + \rho_0 v_{sf}^2 = p_1 + \rho_1 [v_{sf} - u_1(r_{01})]^2$

V. Morel, A. Bultel et al.

[Spectrochim. Acta B 103-104 \(2015\) 112](#)

ANF LIBS – 15 nov. 2021 – A. BULTEL

Collisional-radiative source term

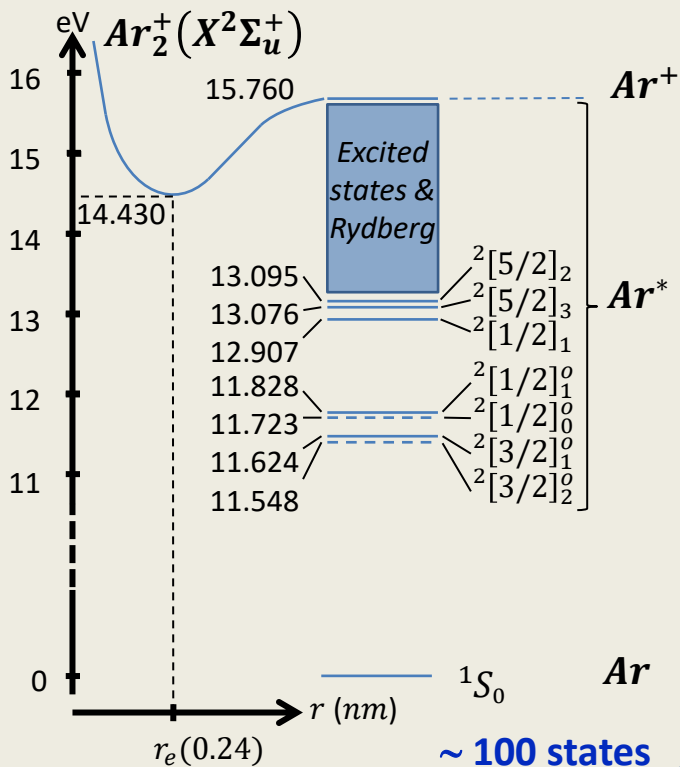
(2) Central plasma

Mass $M_2 = \frac{2\pi}{3} \rho_2 r_{12}^3 \Leftrightarrow \frac{d\rho(\{Al,W\}_j^{Z+})}{dt} = \dot{\rho}(\{Al,W\}_j^{Z+}) - 3\rho(\{Al,W\}_j^{Z+}) \frac{u_2(r_{12})}{r_{12}}$

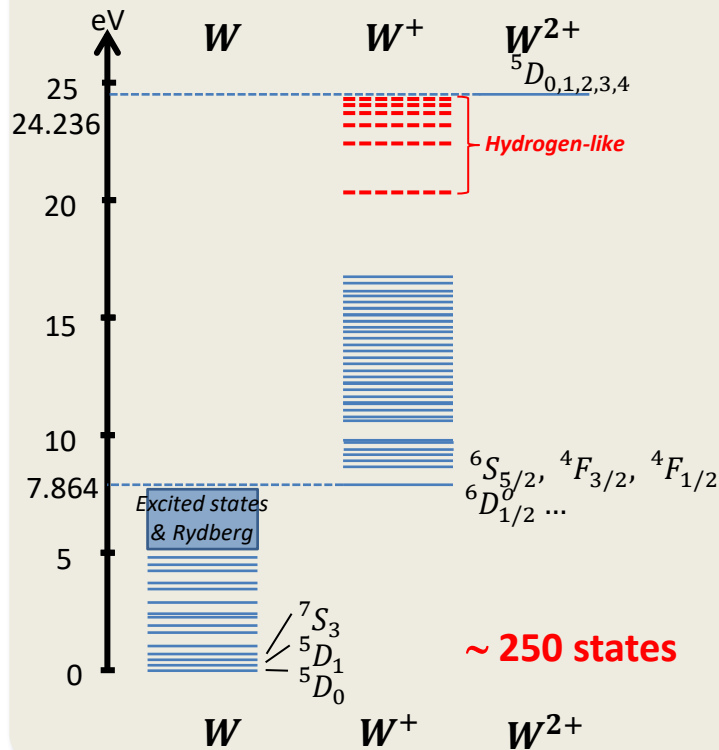
Energy $E_2 = M_2 (\epsilon^{Al,W} + \epsilon_2) + E_{c,2} \Leftrightarrow \frac{dE}{dt} = \rho_0 \epsilon_0 v_{sf}^2 2\pi r_{01}^2 - \frac{M_2}{\rho_2} (4\pi \epsilon_{RR} + 4\pi \epsilon_{TB} + \epsilon'_{SE})$

Momentum $\frac{d[u_2(r_{12})]}{dt} = \frac{8\pi r_{12}^2}{3 M_2} (p_2 - p_1)$

Shock layer - Argon



Central plasma - Tungsten



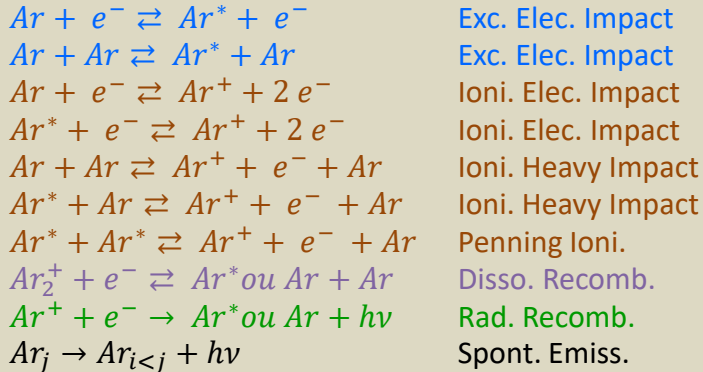
The ECHREM* code

* Eulerian Chemically Reactive
Multi-component plasma code



Shock layer - Argon

Collisional-Radiative model CoRaM-RG



30 000 elementary processes

Collisional Database

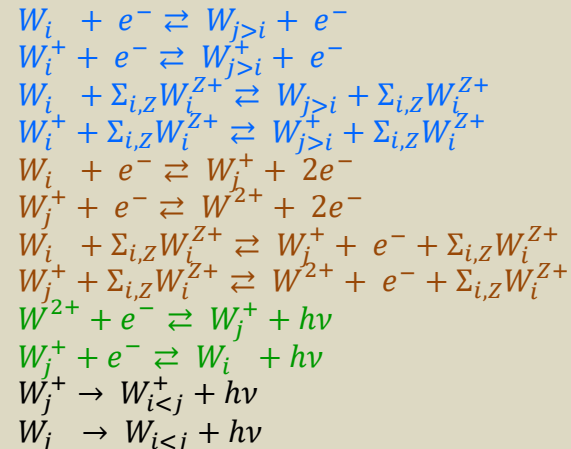
$$k_i(T_{A,e}) = \sqrt{\frac{8 k_B T_{A,e}}{\pi \mu}} \int_{x_0}^{+\infty} x e^{-x} \sigma_i(x) dx \text{ with}$$

- $\sigma_i(x)$ collisional cross section and
- $x = \frac{\varepsilon}{k_B T_{A,e}}$ reduced collision energy

Backward rate coefficient deduced from the *Detailed Balance*

Central plasma - Tungsten

Collisional-Radiative model CoRaM-W



Thermal Bremsstrahlung

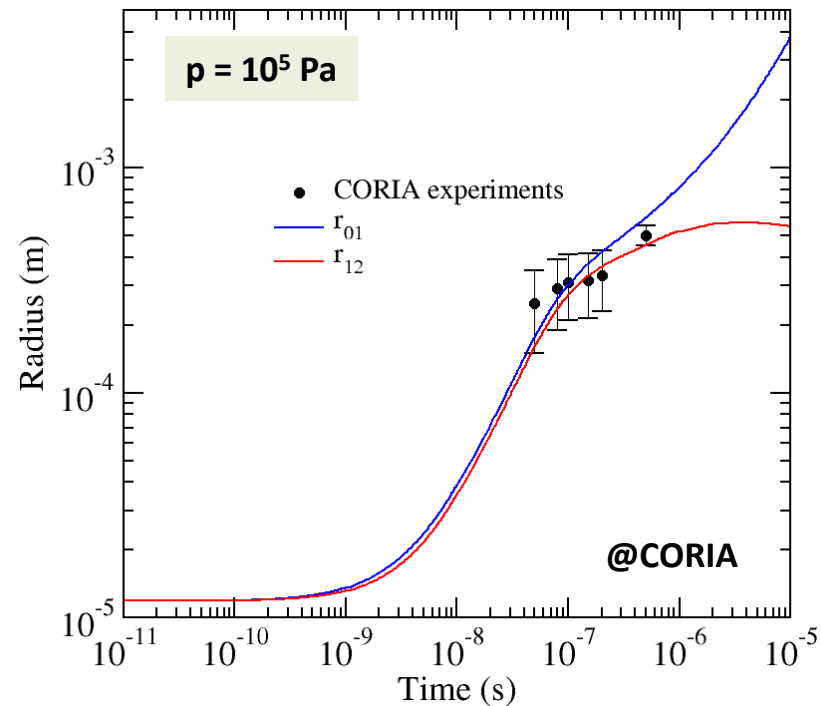
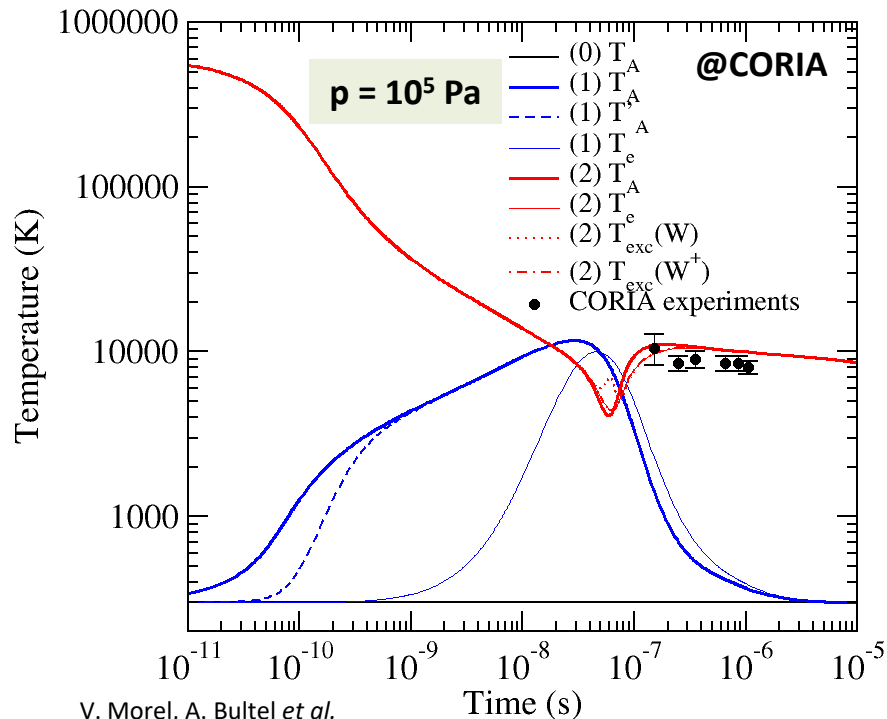
520 000 elementary processes

Radiative Database

NIST, Atomic Line List, ADAS, HULLAC...

The **ECHREM*** code

***Eulerian CHemically REactive**
Multi-component plasma code



V. Morel, A. Bultel *et al.*

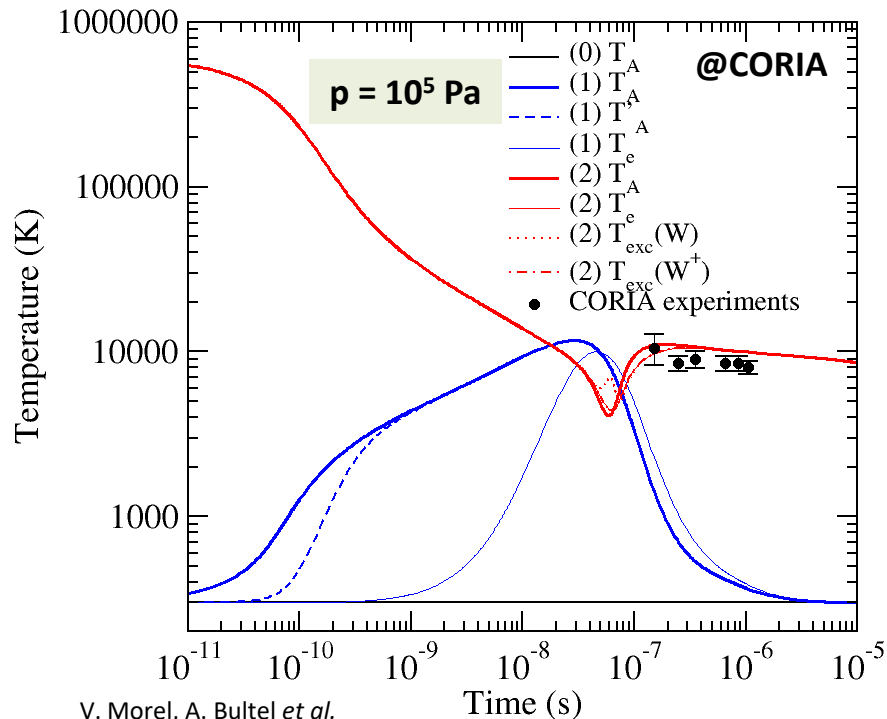
[Spectrochim. Acta B 103-104 \(2015\) 112](#)

ANF LIBS – 15 nov. 2021 – **A. BULTEL**

W (Ar) 10 ps 532 nm 10 J cm⁻²

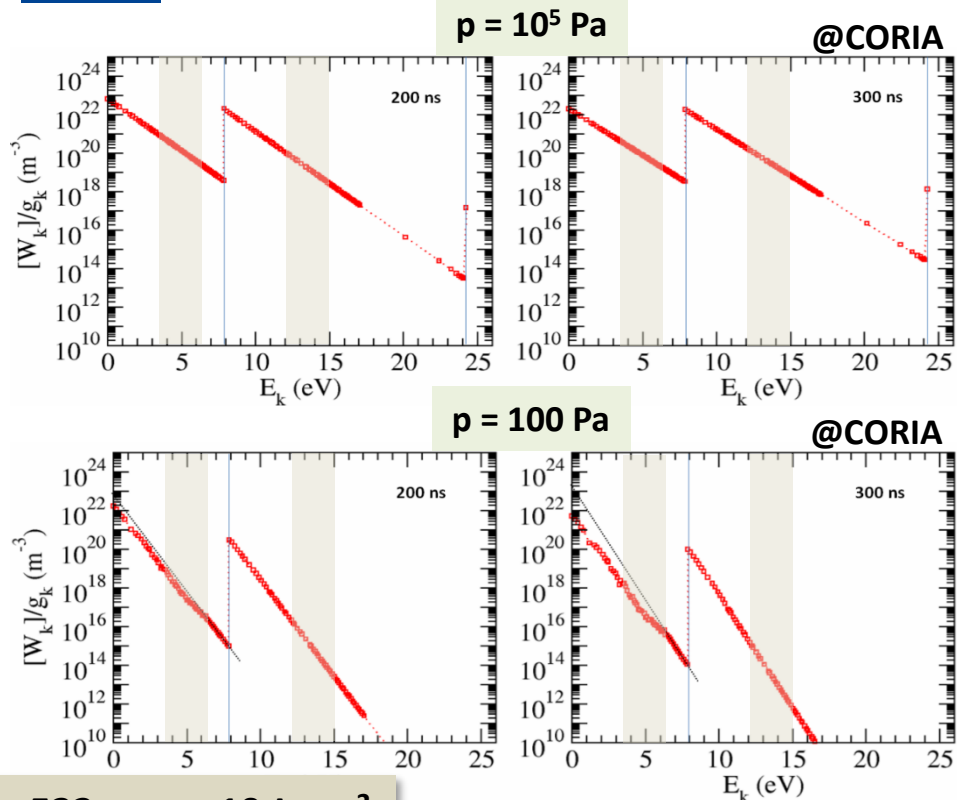
The **ECHREM*** code

* Eulerian **CH**emically **RE**active
Multi-component plasma code



V. Morel, A. Bultel *et al.*

[Spectrochim. Acta B 103-104 \(2015\) 112](#)



W (Ar) 10 ps 532 nm 10 J cm⁻²

McWhirter criterion and other...

McWhirter criterion (1965)

$$n_{e,m^{-3}} > 1,6 \times 10^{18} \sqrt{T_{e,K}} (\Delta E_{ji,eV})_{max}^3$$

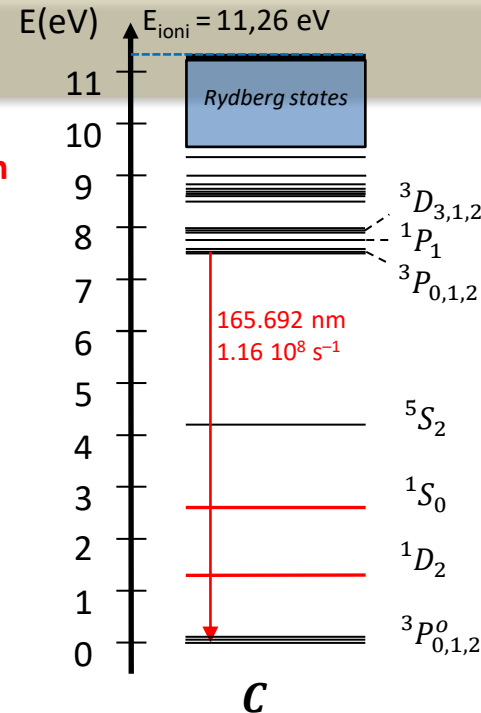
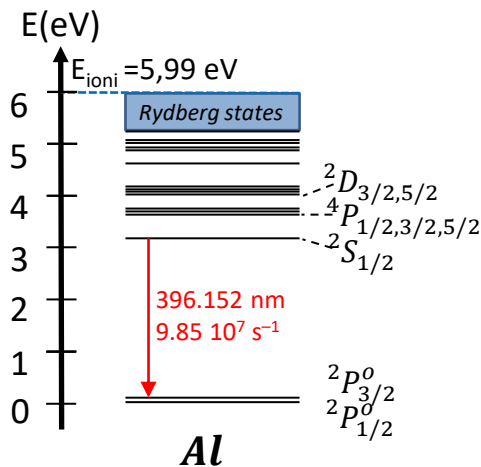
Griem criterion (1963)

$$n_{e,m^{-3}} > 10^{17} \sqrt{T_{e,K}} (\Delta E_{ji,eV})_{rés}^3 Z^7$$

Drawin criterion (1969)

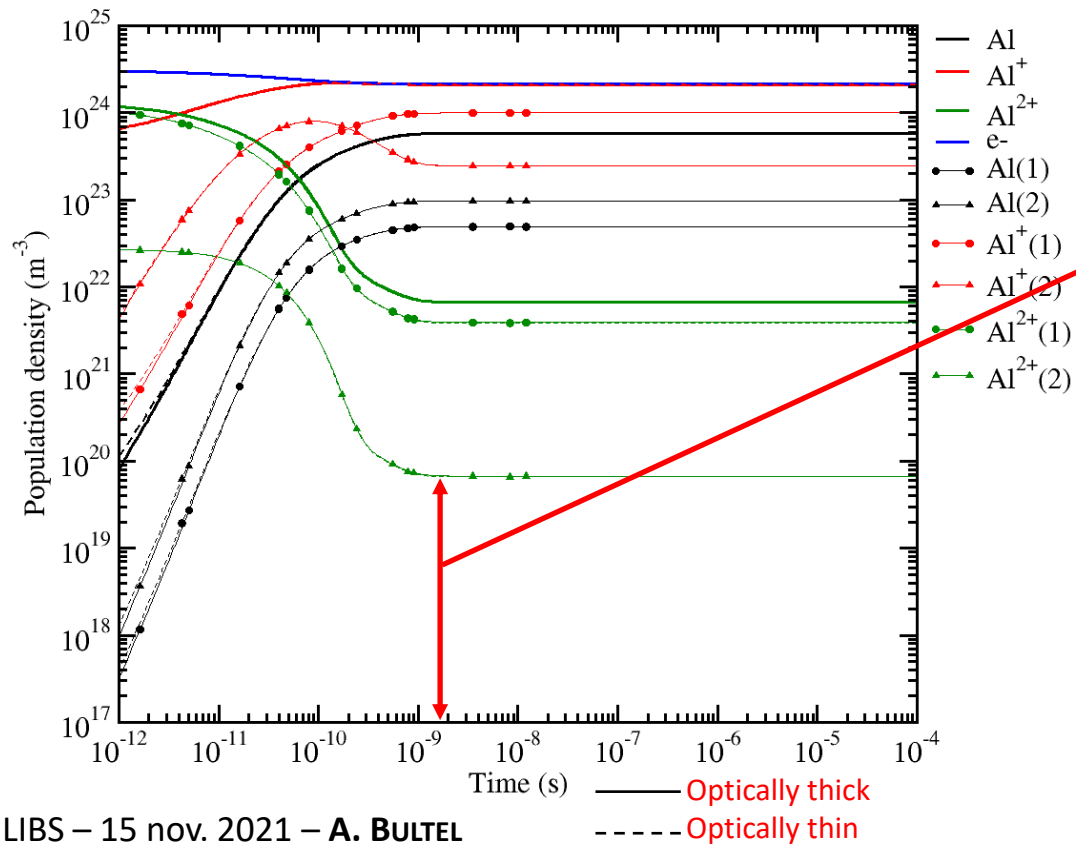
$$n_{e,m^{-3}} > 9,1 \times 10^{16} \sqrt{T_{e,K}} (\Delta E_{ji,eV})_{max}^3 \frac{g_{max}}{g_{min}} \times \begin{cases} 3 \left[\frac{(\Delta E_{ji,eV})_{max}}{T_{e,eV}} \right]^{0,483} & \text{neutres} \\ \left[\frac{(\Delta E_{ji,eV})_{max}}{T_{e,eV}} \right]^{0,269} & \text{ions} \end{cases}$$

Competition collisions (e-) ↔ radiation



Te (K)	15000			
	Al	Al+	C	C+
Z	1	2	1	2
Deji, eV max	3.13	4.64	3.30	5.32
Deji, eV rés	3.14	7.42	7.48	9.29
g_max	2	1	1	2
g_min	4	1	5	4
McWhirter	6.01E+21	1.96E+22	7.04E+21	2.95E+22
Griem	3.79E+20	6.40E+23	5.13E+21	1.26E+24
Drawin	7.86E+20	1.57E+21	3.78E+20	1.23E+21

McWhirter criterion and other...

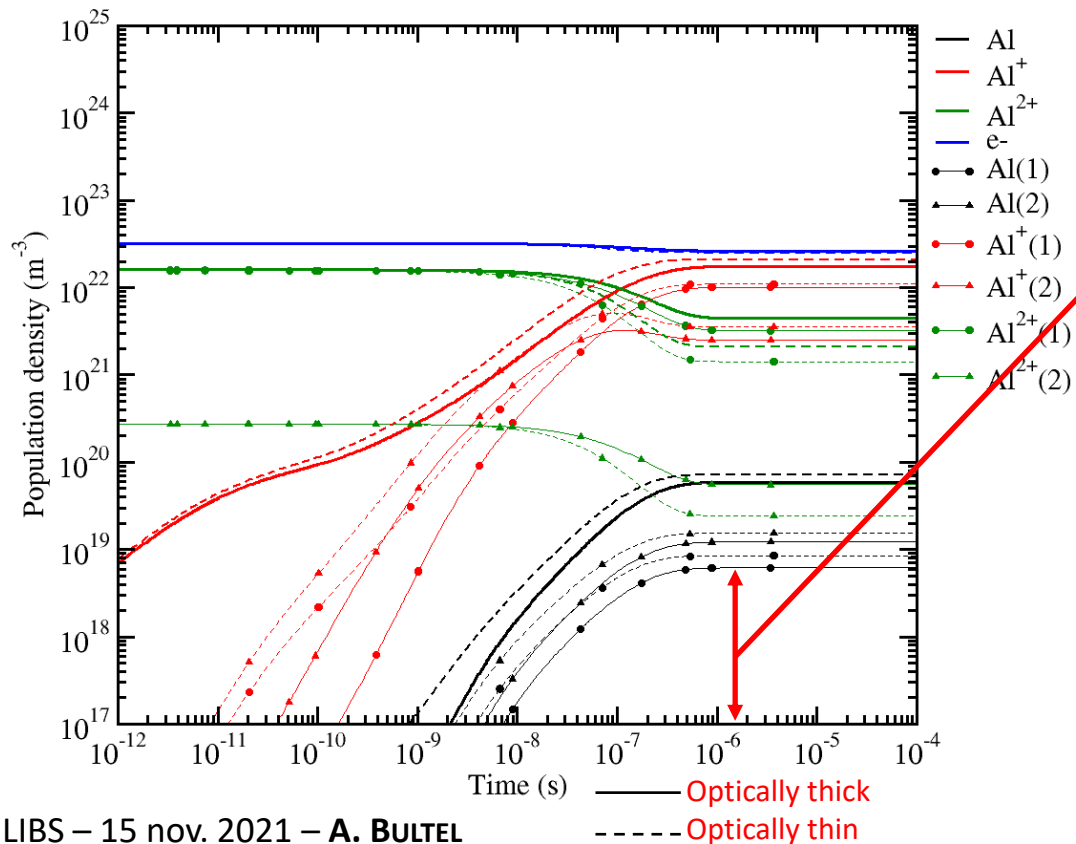


$$p = 10^6 \text{ Pa}, T_e = 15000 \text{ K}$$

- 1. Some 10^{-9} s: steady state
- 2. No radiation influence: final equilibrium state

Te (K)	15000	
Z	Al	Al+
<u>Deji, eV max</u>	3.13	4.64
<u>Deji, eV rés</u>	3.14	7.42
<u>g max</u>	2	1
<u>g min</u>	4	1
<u>McWhirter</u>	6.01E+21	1.96E+22
<u>Griem</u>	3.79E+20	6.40E+23
<u>Drawin</u>	7.86E+20	1.57E+21

McWhirter criterion and other...

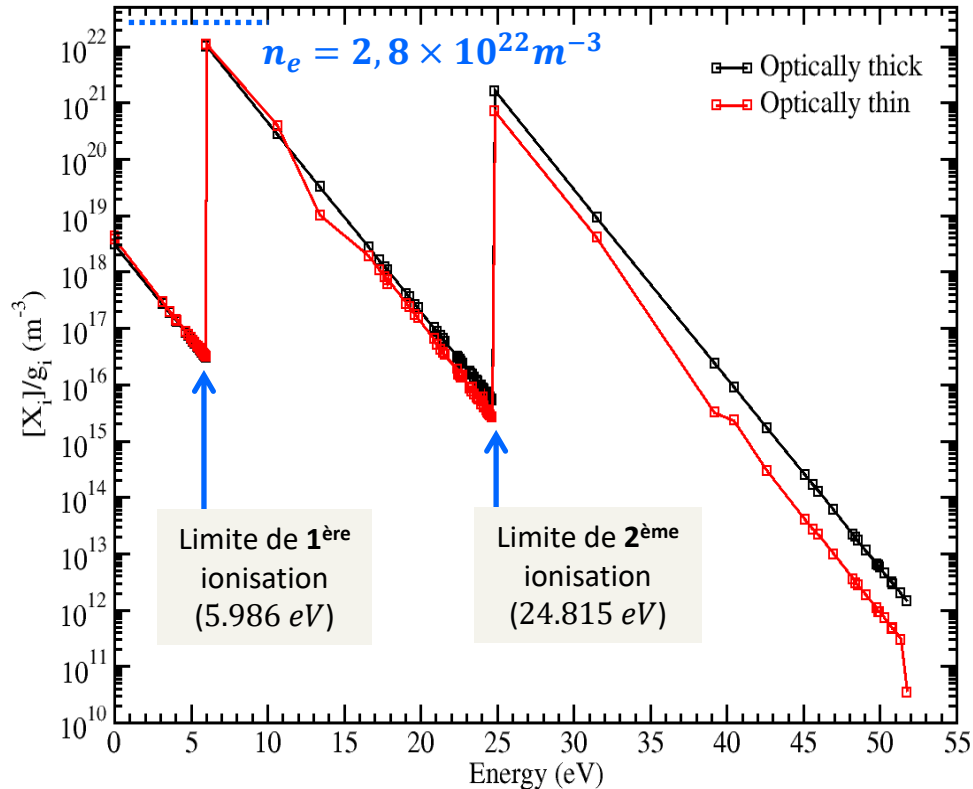


$$p = 10^4 \text{ Pa}, T_e = 15000 \text{ K}$$

1. Some 10^{-6} s: steady state
2. **Strong** radiation influence: final **non** equilibrium state

Te (K)	15000	
Z	Al	Al ⁺
<u>Deji, eV max</u>	3.13	4.64
<u>Deji, eV rés</u>	3.14	7.42
<u>g max</u>	2	1
<u>g min</u>	4	1
<u>McWhirter</u>	6.01E+21	1.96E+22
<u>Griem</u>	3.79E+20	6.40E+23
<u>Drawin</u>	7.86E+20	1.57E+21

McWhirter criterion and other...



$$p = 10^4 Pa, T_e = 15000 K, t = 1 \mu s$$

McWhirter criterion

$$n_{e,m^{-3}} > 1.6 \times 10^{18} \sqrt{T_{e,K}} (\Delta E_{ji,eV})_{max}^3$$

$$n_e > 6,01 \times 10^{21} m^{-3} \text{ for Al}$$

$$n_e > 1,96 \times 10^{22} m^{-3} \text{ for Al}^+$$

Criterion seems to be wrong

$$T_{exc} \neq T_e$$

Te (K)	15000	
Z	Al	Al+
Deji, eV max	3.13	4.64
Deji, eV rés	3.14	7.42
g max	2	1
g min	4	1
McWhirter	6.01E+21	1.96E+22
Griem	3.79E+20	6.40E+23
Drawin	7.86E+20	1.57E+21

